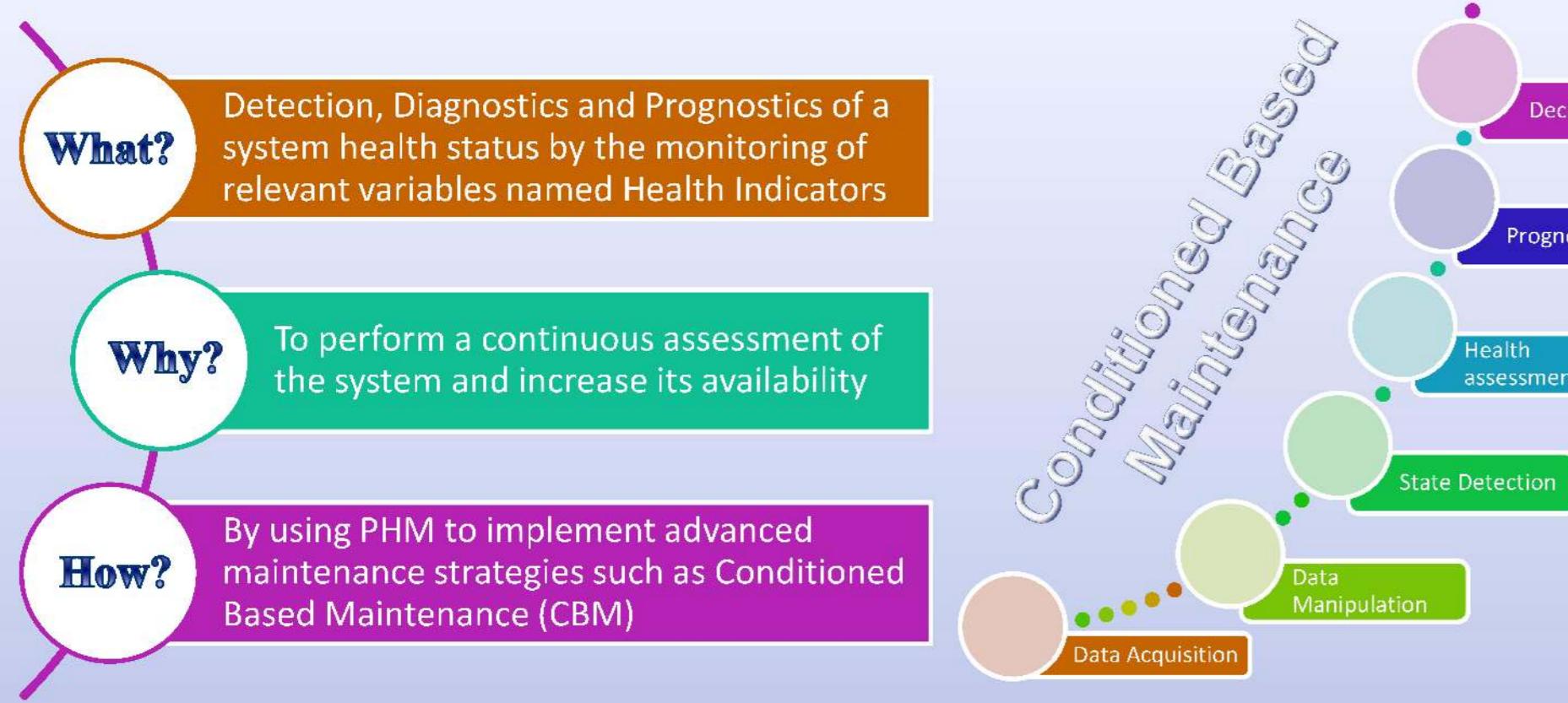
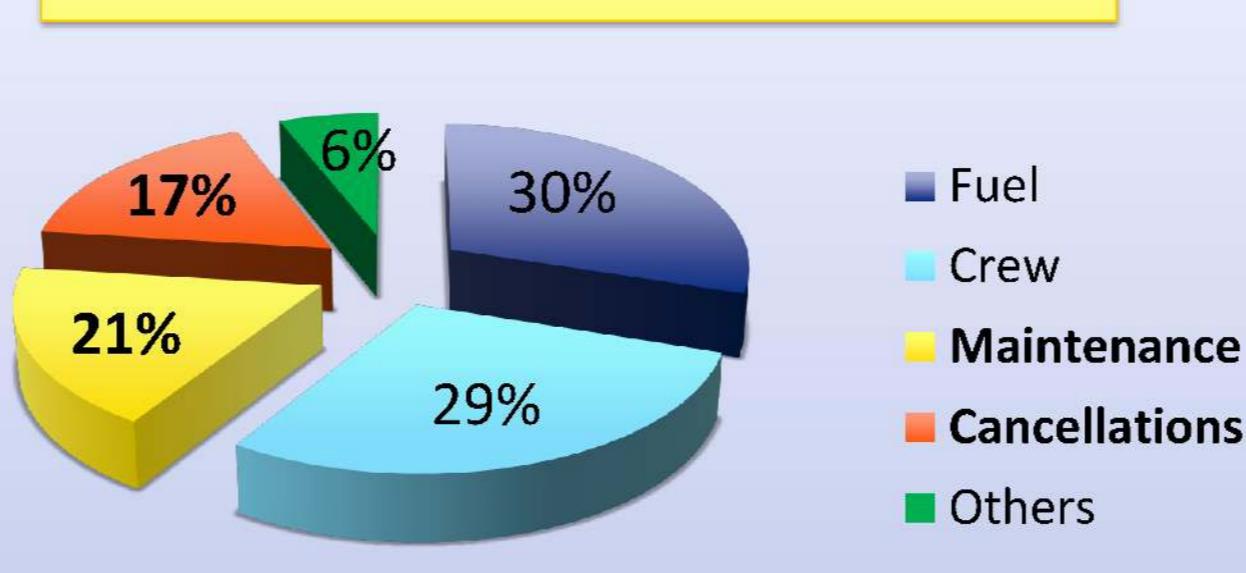


### GENERAL BACKGROUND

#### → Prognostic and Health Management



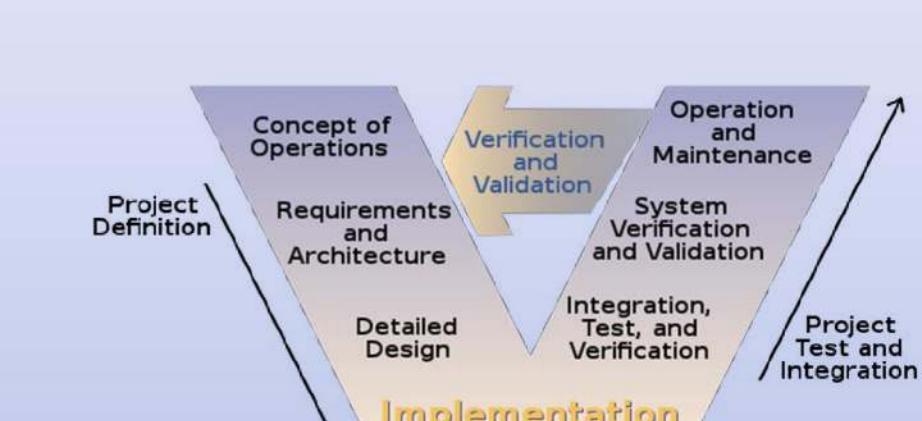
**Main Purpose : Reduction of maintenance-related costs**



**Tool: Prognostic and Health Management**

#### → Main Issues:

1. PHM System Development Framework
2. PHM System Design
3. PHM System Validation
4. Health Indicators Construction
5. Health Indicators Validation
6. Mathematical Methods and Tools

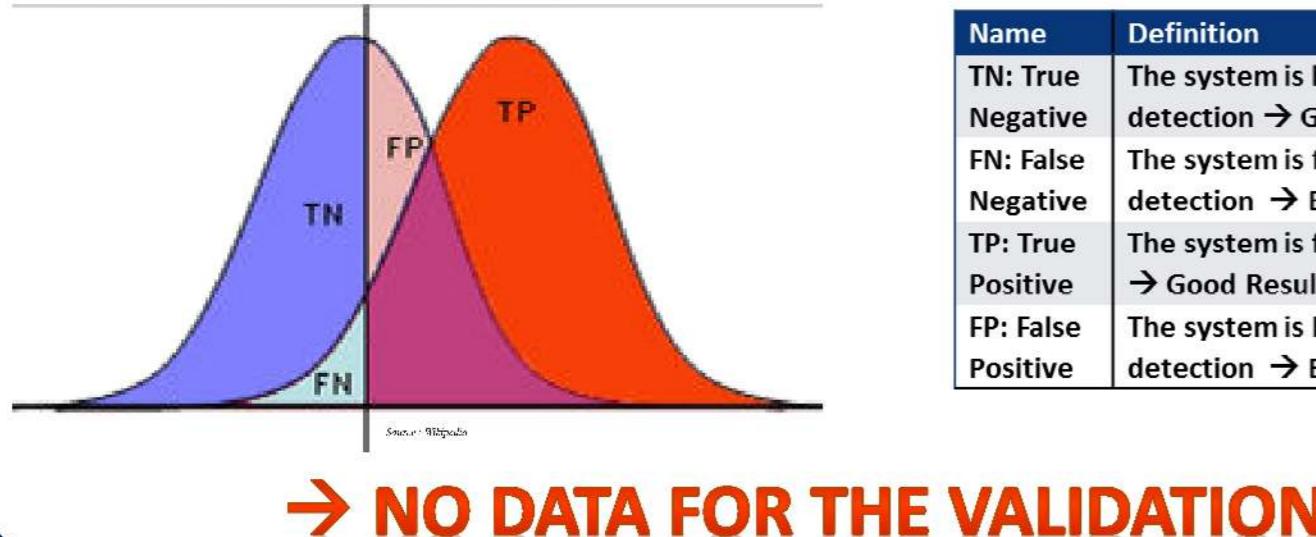


### INTEGRATED PHM

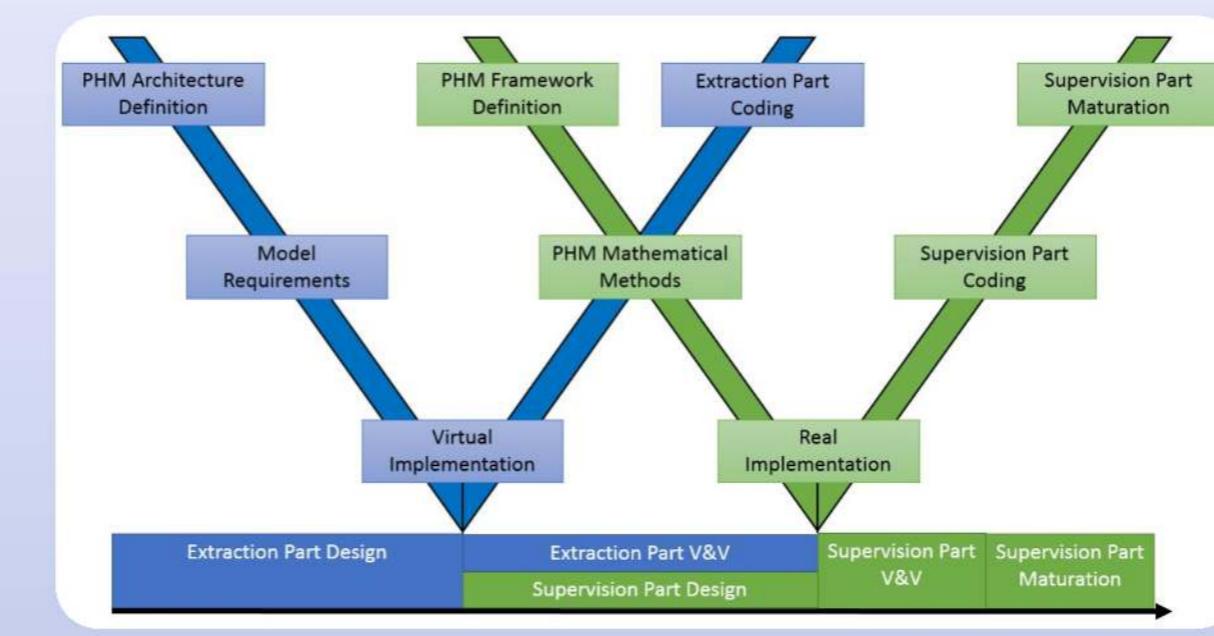
#### 1/ Extraction Part – Upstream Stage

- When? Before the system implementation
- What? - Health Indicators Definition and Validation  
- Extraction Algorithms Coding
- How? By using Numerical KPI for validation

#### → Detection Theory:



**New Proposal: Integrated PHM**  
*To optimize PHM system capabilities at each stage of the development process*



#### 2/ Supervision Part – Downstream Stage

- When? After the system entry into service
- What?  
- PHM system Definition and Validation  
- Supervision Framework Coding  
- PHM Maturation
- How?  
- By using advanced mathematical tools for detection and identification and Operational KPI for validation

**→ LACK OF DEGRADED DATA FOR VALIDATION**

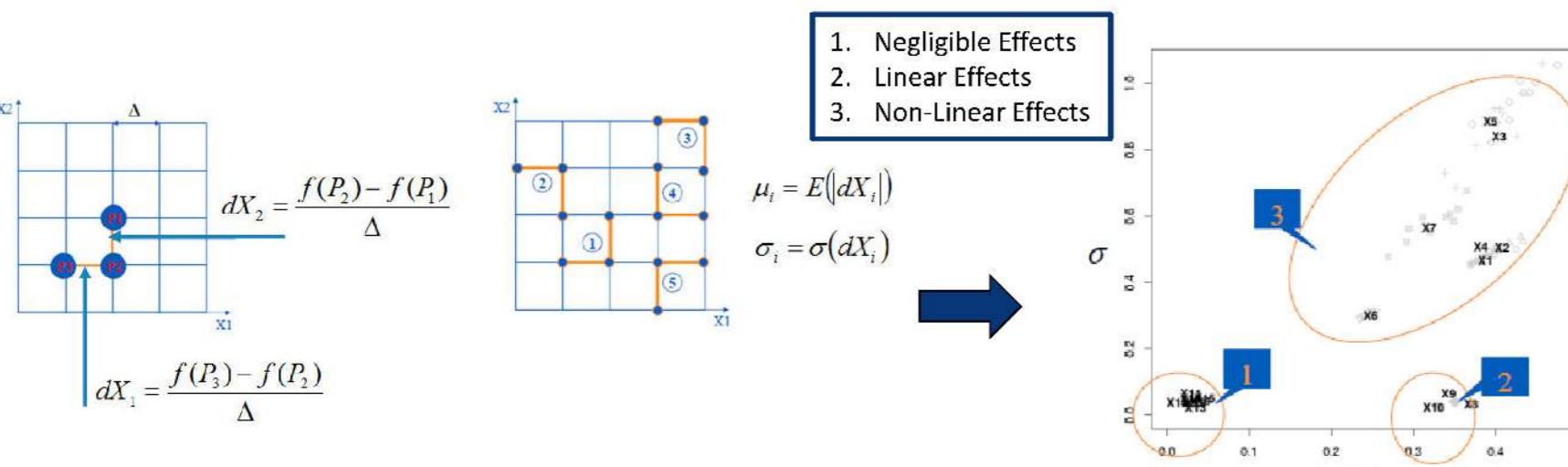
### MODELING

#### Difficulty 1 : managing multiple parameters

→ Sensitivity Analysis for parameters prioritization

##### A. Morris Method

→ One at the time method



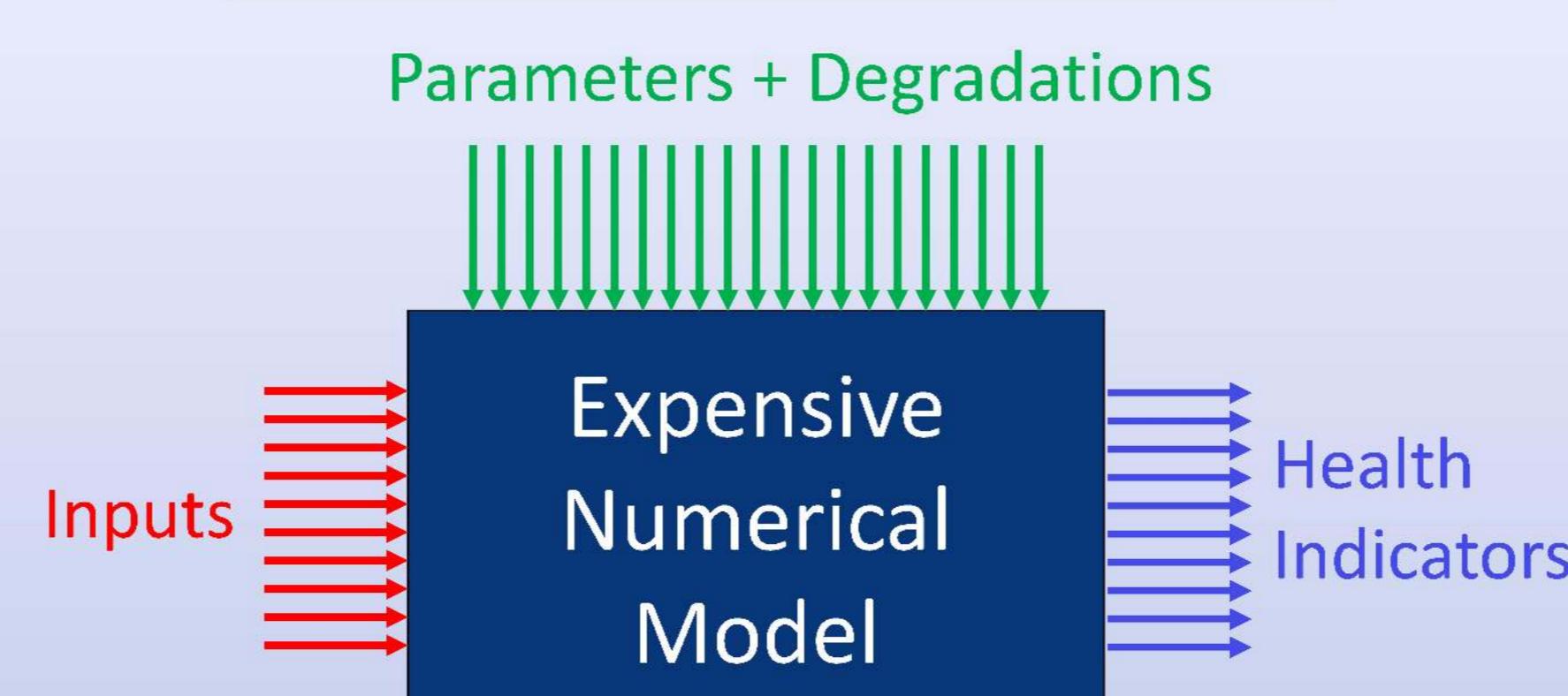
##### B. Sobol Indices

→ Based on Variance Decomposition

→ More precision but more simulations needed

$$S_i = \frac{\text{Var}[\mathbb{E}(Y|X_i)]}{\text{Var}(Y)} = \frac{\mathbb{V}_i(Y)}{\text{Var}(Y)}, \quad S_{ij} = \frac{\mathbb{V}_{ij}(Y)}{\text{Var}(Y)}, \quad S_{ijk} = \frac{\mathbb{V}_{ijk}(Y)}{\text{Var}(Y)}$$

**Solution: Numerical Modeling**  
*To create the data needed for the validation of the PHM Framework*



#### Difficulty 2 : managing uncertainties

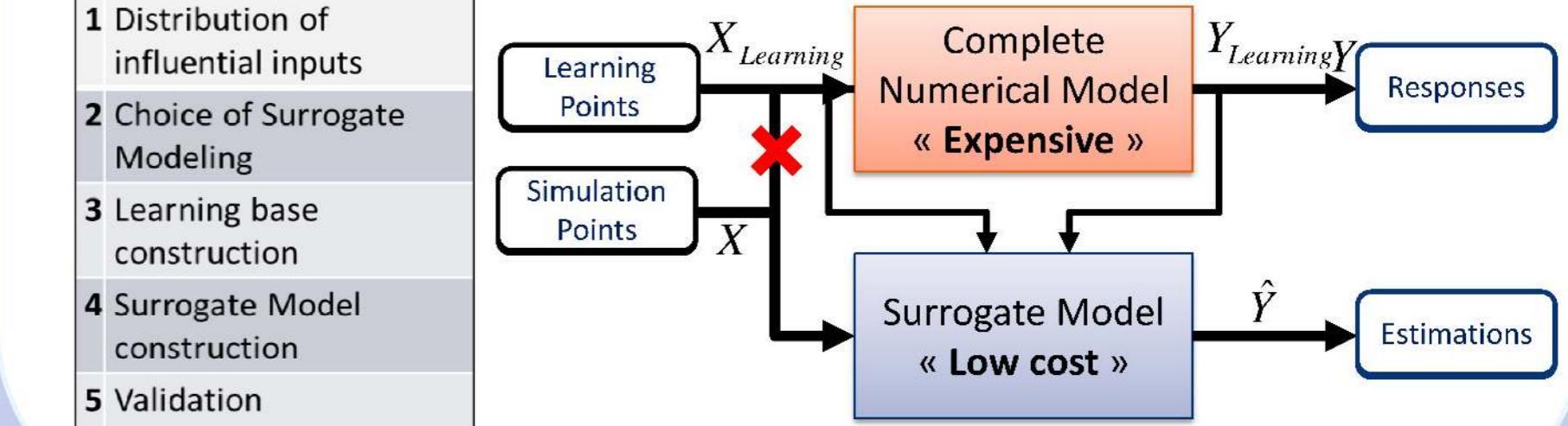
→ Uncertainties Quantification by expertise and experience feedback

→ Uncertainties Propagation to introduce parameters variability into the model

##### A. Monte-Carlo Algorithm

→ too many simulations

##### B. Less expensive Method : Surrogate Modeling



### APPLICATIONS

#### Surrogate Modeling

**Sensitivity analysis: Morris Method**

**Surrogate Modeling: Latin Hypercube + Kriging**

##### A. Sensitivity Analysis

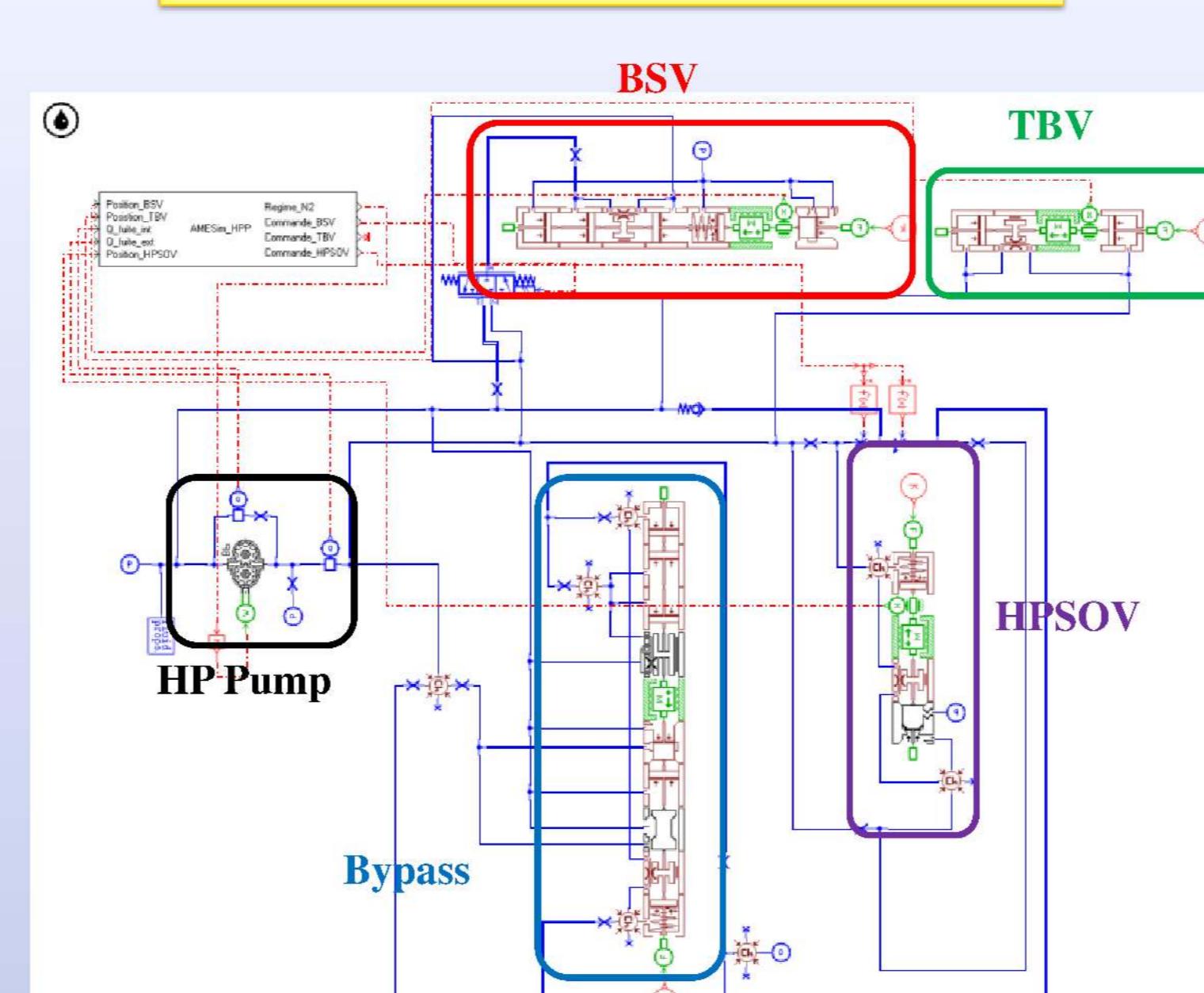
- Morris Method → 220 simulations
- Originally 43 parameters
- Reduction to 20

##### B. Kriging

- Kriging Model:  $Y(x) = f^T(x) \cdot b + Z(x)$
- $f^T(x) \cdot b$  regression model
- Z Gaussian process:  
- > of mean zero  
- > of covariance  $\sigma^2 R(\theta, w, x)$   
- > with R correlation function:  
 $R(\theta, w, x) = \prod_{j=1}^n R_j(\theta, w_j - x_j)$

$$\text{Exponential correlation: } R_j(\theta, w_j - x_j) = \exp(-\theta_j \cdot |w_j - x_j|)$$

#### High Pressure Fuel Pump PHM



#### Numerical Key Performance Indicators

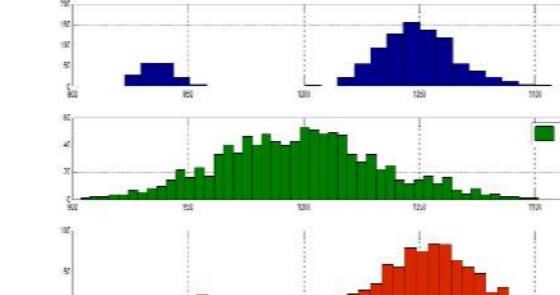
**Health Indicator :** Engine Rotation speed at BSV, TBV and HPSOV Opening → wBSV, wTBV and wHPSOV

**Degradations :** HP Pump Internal Leakage

##### A. Health Indicators distributions

→ Surrogate model + Monte-Carlo simulations

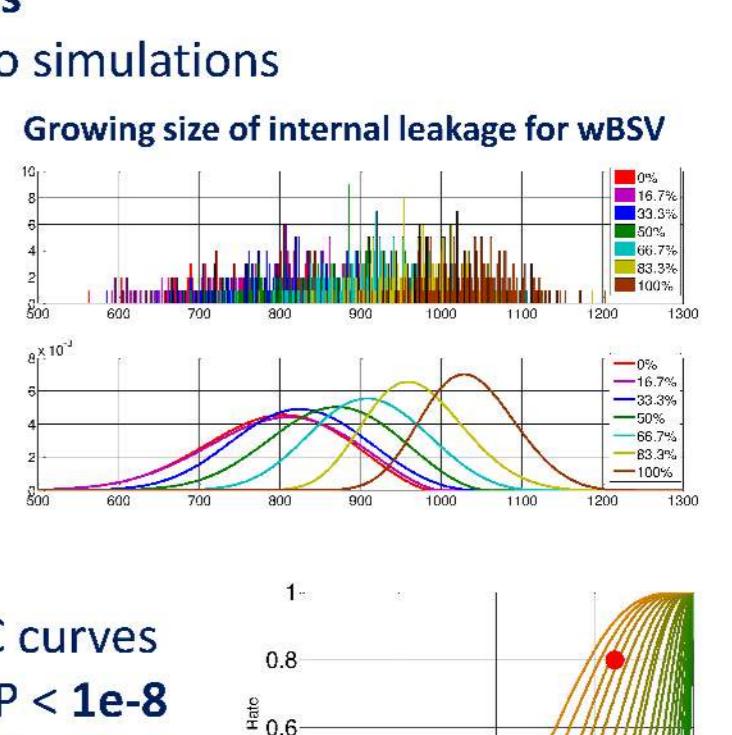
**Healthy state for wTBV**



**B. Numerical KPI:**

- Based on semi-logarithmic ROC curves
- Common Criteria : TP > 0.8 & FP < 1e-8
- Compliance Point (CPT) : (FP;TP)

$$\text{NKPI : Compliant Detectability } CDet = \begin{cases} 1 & \text{if the curve is above the CP} \\ 0 & \text{if the curve is under the CP} \end{cases}$$



#### → Publications:

- ✓ Massé, J.R., Lamoureux, B., & Boulet, X. (2011). *Prognosis and Health Management in System Design*, IEEE PHM 2011 proceedings,
- ✓ Lamoureux, B., Massé, J.R., & Mechbal, N. (2012). *An approach to the Health Monitoring of the Fuel System of a Turboprop*, IEEE PHM 2012 proceedings.
- ✓ Lamoureux, B., Massé, J.R., & Mechbal, N. (2012). *Methodology for the Diagnosis of Hydromechanical Actuation Loops in Aircraft Engines*, 20th Mediterranean Conference on Control and Automation proceedings.
- ✓ Lamoureux, B., Massé, J.R., & Mechbal, N. (2012). *An Approach to the Health Monitoring of a Pumping Unit in an Aircraft Engine Fuel System*, First European Conference of the Prognostics and Health Management Society proceedings.

#### → Bibliography

- ✓ Aurousseau, C., et al. (2007). *Surveillance d'une Pompe Haute-Pression dans un Circuit d'Alimentation en Carburant d'une Turbomachine*, brevet 0708099.
- ✓ De Rocquigny, E., Devictor, N., Tarantola, S., Mangeant, F., Schwob, C., Bolado-Lavin, R., Massé, J. R., Limbourg, P., Kanning, W. and Van Gelder, P. (2007). *Uncertainty in industrial practice: A guide to quantitative uncertainty management*, Wiley.
- ✓ Kleijnen, J. P. C. (2009). *Kriging metamodeling in simulation: a review*, European Journal of Operational Research, vol. 192, n° 13, pp. 707-716.
- ✓ Morris, M. D. (1991). *Factorial sampling plans for preliminary computational experiments*, Technometrics, vol. 33, pp. 161-174.
- ✓ Wickens, T. D. (2002). *Elementary Signal Detection Theory*, Oxford University Press.